

# Pi2 Pulsations During Extremely Quiet Geomagnetic Condition: Van Allen Probe Observations

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A ultra low frequency (ULF) wave, Pi2, has been reported to occur during periods of extremely quiet magnetospheric and solar wind conditions. And no statistical study on the Pi2 has been performed during extremely quiet conditions, using satellite observations to the author's knowledge. Also Pi2 pulsations in the space fluxgate magnetometers near perigee failed to attract scientist's attention previously. In this paper, Pi2 pulsations detected by the Van Allen probe satellites (VAP-A & VAP-B) were investigated statistically. During the period from October 2012 to December 2014, ninety six Pi2 events were identified using VAP when  $K_p = 0$  while using Kakioka (KAK,  $L = 1.23$ ) as a reference ground station. Seventy five events had high coherence between VAP-Bz and H components at KAK station. As a result, it was found that 77 % of the events had power spectra between 5 and 12 mHz, which differs from the regular Pi2 band range of from 6.7 to 25 mHz. In addition, it was shown that it is possible to observe Pi2 pulsations from space fluxgate magnetometers near perigee. Twenty two clean Pi2 pulsations were found where  $L < 4$  and four examples of Pi2 oscillations at different L shells are presented in this paper.

**Keywords:** Pi2 pulsation, Van Allen probe satellites, extremely quiet condition

## 1. INTRODUCTION

Phenomena of Pi2 magnetic pulsations (6.7 to 25 mHz - 40 to 150 sec) are associated with the substorm onset. The excitation of Pi2 pulsation is still one of the important subjects in the area of the magnetospheric ultra low frequency waves. The main characteristics of Pi2 pulsations are as follows: (1) they are observed at nightside and dayside region (Sutcliffe & Yumoto 1989, 1991; Ghamry et al. 2011, 2012; Ghamry & Fathy 2016); (2) they are, in general, compressional events (Lee 1998); (3) they are detected in the low-latitude regions ( $L < 5$ ) on both ground-based and space measurements (Lee 1998). Yeoman & Orr (1989) showed there are a couple of modes for the Pi2 generation mechanisms. The first is the plasmopause surface wave (Sutcliffe 1975) and the second mechanism is the plasmaspheric cavity mode (Allan et al. 1986; Zhu & Kivelson 1989; Fujita & Glassmeier 1995; Lee 1996). Kepko & Kivelson (1999) showed that the mid-latitude/low-latitude Pi2 pulsations can be driven by fast-mode pulses in the near-Earth magnetotail. Takahashi et al. (2001, 2003)

reported the excitation of cavity mode properties in the inner magnetosphere based on satellite observations. Teramoto et al. (2011) used cluster satellites inside the plasmasphere and a satellite in the plasmatrough to provide additional evidence of plasmaspheric virtual resonance based on observations of the Pi2 pulsations using two satellites at different regions in the inner magnetosphere. Ghamry et al. (2015) made an observation for Pi2 pulsations using Van Allen probes (VAP-A & VAP-B). According to the study show, the Pi2 pulsations observed outside the plasmasphere support the plasmaspheric virtual resonance model.

Although Pi2 can be associated with substorms, Pi2 can also occur with periods and waveforms similar to classical Pi2 pulsations without the occurrence of substorms. Sutcliffe (1998) reported Pi2 pulsation that occurred during quiet conditions on 10 March 1997. Lyons et al. (1999) investigated quiet-time Pi2 pulsations in detail. Kwon et al. (2013) statistically examined the quiet-time Pi2 events observed on a ground station in South Korea, in the year 2008. Ghamry (2015) reported a

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morningside Pi2 pulsation that occurred in the absence of substorm in very quiet geomagnetic conditions ( $K_p = 0$ ). Kwon et al. (2015) studied the plasmapause location in the period of quiet geomagnetic conditions using the electron density from the time history of events and macroscale interactions during substorms (THEMIS). Until now, however, there is no statistical study of the Pi2 pulsations using satellite observations during extremely quiet conditions when  $K_p = 0$  to the best of the author's knowledge. Also, no attention has been paid to Pi2 pulsation in the space fluxgate magnetometers near perigee. In this study, a statistical investigation on the Pi2 pulsations observed under the very quiet geomagnetic conditions ( $K_p = 0$ ) using Van Allen probe satellites for the period from October 2012 to December 2014. All of Pi2 events detected did not show sudden decreases in auroral electrojet index AL. Also, Pi2 pulsation in the space magnetometers near perigee was studied.

The organization of the paper is as follows. Section 2 describes the data sets and Section 3 presents an example of Pi2 pulsations when  $K_p = 0$ . The statistical analysis is described in Section 4. In Section 5, twenty two Pi2 pulsations where  $L < 4$  are presented. In Section 6, we discuss the results and Section 7 gives the conclusions.

## 2. DATA SETS

By using Kakioka (KAK,  $L = 1.23$ ) magnetic field records in Japan as a reference signal to identify Pi2 pulsations, observation was made during extremely quiet geomagnetic conditions ( $K_p = 0$ ), in the nighttime (1800-0600 local time;  $LT = UT + 9$  hours). Then the Pi2 events occurred in the nighttime (1800- 0600 magnetic local time) at Van Allen probes (VAP-A & VAP-B) were visually examined to exclude waves excited by solar wind disturbances. The twin Van Allen probe (VAP) spacecraft, launched on 30 August 2012, makes a near-equatorial orbit with apogee ( $L \sim 6 R_E$ ) and perigee ( $L \sim 700$  km) (Mauk et al. 2013).

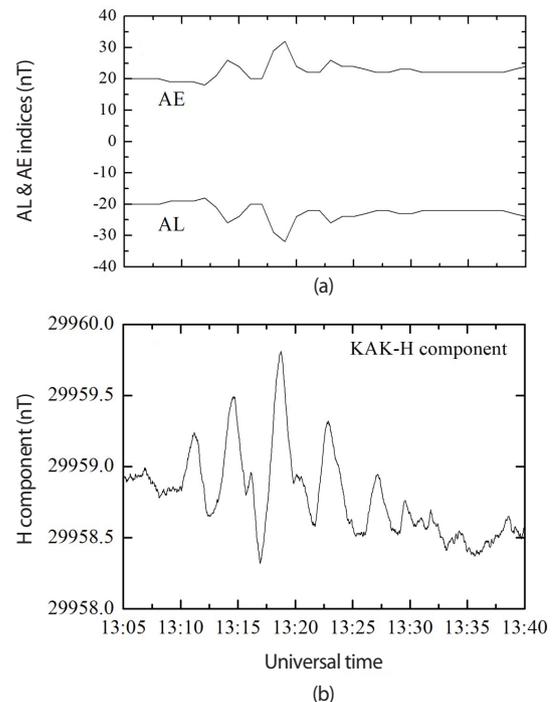
VAP consists of two spacecrafts (VAP-A and VAP-B) and both have identical triaxial fluxgate magnetometers capable of measuring 64 vectors per second (Kletzing et al. 2013). Electric and magnetic field instrument suite and integrated science (EMFISIS) (Kletzing et al. 2013) was used to get magnetic field data. We rotated the EMFISIS magnetic field data of the geocentric solar magnetospheric (GSM) coordinate system into a mean field aligned (MFA) coordinate system. This decomposition allows the dominant magnetic field wave polarization to be determined as toroidal (azimuthal), poloidal (radial), or compressional (parallel). In this system,  $E_z$  is in the direction of the mean magnetic field,  $E_y$  (eastward)

is parallel to  $E_z \times r$ , where  $r$  is the position vector of the satellite relative to the center of the Earth; and  $E_x$  (radial) is given by  $E_x = E_y \times E_z$ .

The electric field data were provided in the modified geocentric solar ecliptic (MGSE) coordinates in which  $E_y$  and  $E_z$  are in the satellite spin plane, with  $E_y$  pointing duskward (nearly the same as  $Y_{gse}$ ), and  $E_z$  pointing nearly along the positive normal to the ecliptic. The  $y$  and  $z$  components in MGSE were measured directly by electric field and waves (EFW) instrument (Wygant et al. 2013). The parallel component,  $\delta B_z$  defined by  $B_z$  (1 sec) minus  $B_z$  (5 min average) is the high-pass filtered compressional component. The data has different resolution for the components. It is 1 sec for the VAP magnetic field, 11 sec for the VAP electric field and 1 sec for the KAK magnetic field. For frequency domain analysis, 12 sec averages for all components are used.

## 3. AN EXAMPLE OF Pi2 PULSATIONS WHEN $K_p = 0$

The provisional auroral electrojet index AL & AE and the horizontal component of the magnetic field H (northward), from KAK, as shown in Figs. 1(a) and 1(b), respectively, from 13:05 to 13:40 UT on 31 December 2012. AE index ranges from -20 nT at 1308 UT to -31 nT at 1317 UT. Although AL is negative, its magnitude is small ( $< 34$  nT), and decreases during a typical substorm. Therefore, a substorm current wedge was



**Fig. 1.** (a) The auroral electrojet AL and AE indices and (b) H component at KAK from 1305 to 1340 UT on 31 December 2012.

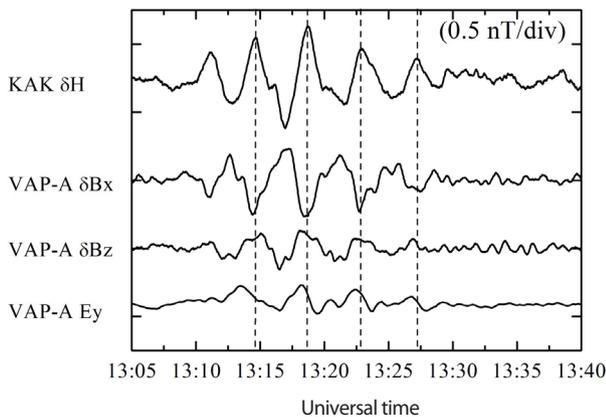
not formed during the Pi2 event (Clauer & McPherron 1974). As per this observation, it is suggested that the Pi2 pulsation presented in Fig. 1 occurred in the absence of a substorm.

Space observations are important to examine the properties of magnetic and electric field perturbations in space which correspond to Pi2 pulsations on the ground. We have compared the low latitude horizontal H component on the ground and the poloidal components in space which are characterized by the azimuthal oscillation of the electric field ( $E_y$ ), the radial ( $\delta B_x$ ) and compressional ( $\delta B_z$ ) oscillations of the magnetic field in Fig. 2. To identify the phase delay, the vertical dashed lines in Fig. 2 is drawn through the peaks of  $\delta H$  component.

During the time of interest (UT = 13:05-13:40), the VAP-A was in south of the magnetic equator with a magnetic latitude between  $-9.28$  and  $-9.72$ , and it moved outward from  $L = 4.0$  to  $L = 4.8$  post-midnight while KAK was in pre-midnight. Both the VAP-A and KAK were found on the night side separated by a small local time ( $\sim 3$  hours).

As shown in Fig. 2, VAP-A observed a compressional ( $\delta B_z$ ) component with period and waveform similar to the H component at KAK. This gives us an indication that the oscillations at KAK and VAP-A are excited by a similar source. The radial magnetic field component,  $\delta B_x$ , at VAP-A oscillates out of phase with  $\delta B_z$ . The vertical dashed lines, in Fig. 2, indicate that the  $\delta B_z$  peaks precede the  $E_y$  peaks by a quarter of the wave period, which is equivalent to a phase delay of  $\sim 90^\circ$ . These phase relationships among the poloidal components ( $\delta B_x$ ,  $\delta B_z$ , and  $E_y$ ) are considered as an indication to the fundamental mode (Takahashi et al. 2001, 2003). One can note that  $\delta B_x$  is larger than  $\delta B_z$  by a factor of  $\sim 2$ . It is believed that VAP-A was near the node in the fundamental mode  $\delta B_z$  perturbation (Takahashi et al. 1995).

The frequency analysis was used in this study because it gives additional details on the frequency dependence of the

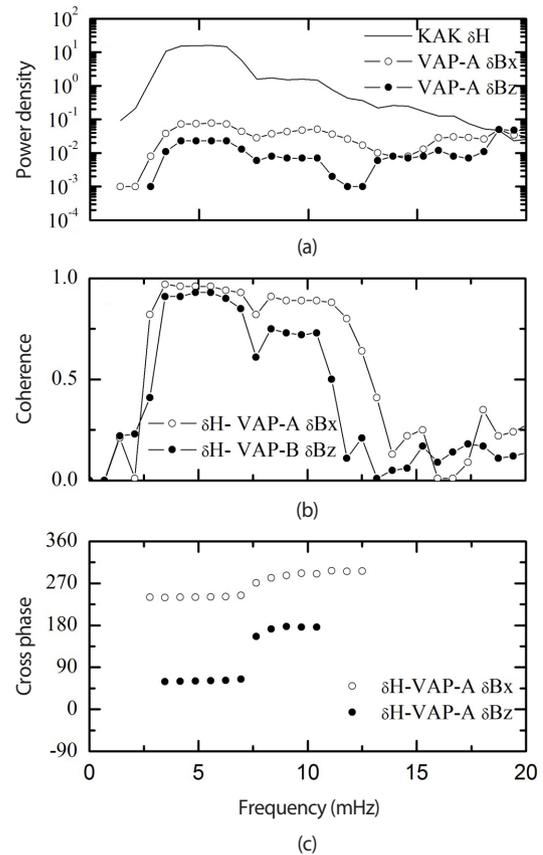


**Fig. 2.**  $\delta H$  component at KAK and  $\delta B_x$ ,  $\delta B_z$ , and  $E_y$  measured by VAP-A from 1305 to 1340 UT on 31 December 2012.

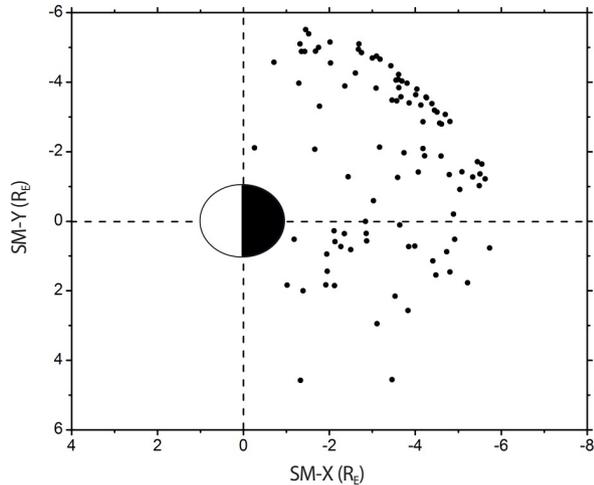
coherence and cross phase. We compute the power spectral density, coherence, and cross phase for the 35 min interval from 1305 UT to 1340 UT using Fourier transform with five point smoothing in the frequency domain. The cross phase is calculated for frequencies at which the coherence is greater than 0.7. The spectral parameters are plotted in Figs. 3(a)-3(c). The  $\delta B_z$  data from VAP-A show a power spectrum similar to the KAK spectrum in the frequency band from 3 to 12 mHz. In this band, the coherences of KAK-VAP-A  $\delta B_z$  and KAK-VAP-A  $\delta B_x$  are higher than 0.7. The Fig. 3(c) show a mixture of the fundamental ( $\sim 4$  mHz) and second harmonic ( $\sim 8$  mHz). The cross phase between KAK-VAP-A  $\delta B_z$  and KAK-VAP-A  $\delta B_x$  are about  $180^\circ$  and about  $270^\circ$ , respectively.

#### 4. STATISTICAL RESULTS

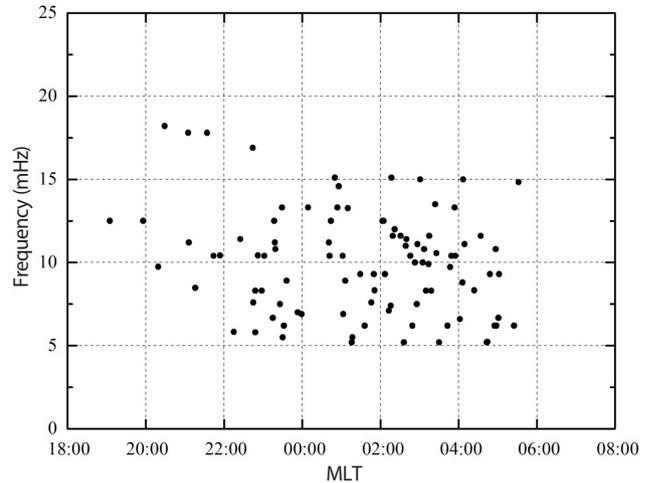
A statistical analysis of the ninety six Pi2 pulsations identified by VAP-A and VAP-B was performed. Fig. 4 illustrates the location of the VAP in the SM (solar magnetic) coordinates for all Pi2 events. Fig. 5 shows the ninety six events distribution



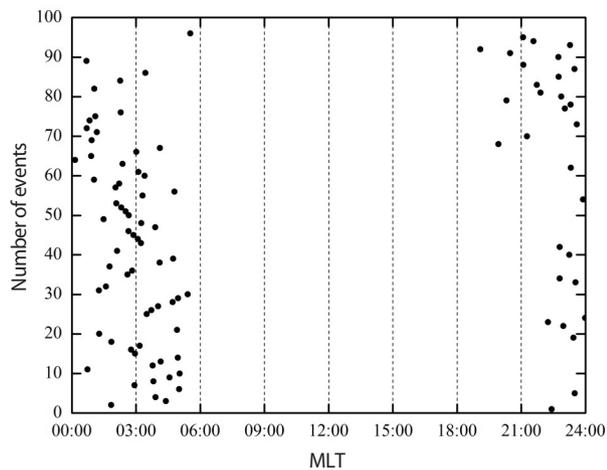
**Fig. 3.** spectral properties of KAK  $\delta H$  component, VAP-A  $\delta B_x$ , and VAP-A  $\delta B_z$  components from 1305 to 1340 UT on 31 December 2012 (a) power spectra (b) coherence (c) cross phase.



**Fig. 4.** Location of the VAP in the solar magnetic (SM) coordinates for all Pi2 pulsations.



**Fig. 6.** Pi2 frequency distribution based on magnetic local time (MLT).



**Fig. 5.** Distribution of all Pi2 events based on magnetic local time (MLT).

according to magnetic local time (MLT). In Fig. 5, the Pi2 events are distributed from 01:00 to 05:00 MLT, and relatively small number of pulsations are observed from 19:00 to 00:00 LT.

Fig. 6 shows the Pi2 frequency distribution based on magnetic local time. We found seventy five events have power spectra ranging from 5 to 12 mHz, which differ from the regular Pi2 band range from 6.7 to 25 mHz (Troitskaya 1967). The Pi2 power has the highest value at 20-23 MLT, and there was an asymmetry phenomenon of Pi2 power around the midnight. We examined the coherence between KAK H and the poloidal components at VAP. We found seventy five pulsations with high coherence between VAP and H components at KAK station. In this study, the meaning of high coherence is that the H component at KAK and one of the poloidal components at VAP satellite have spectral peaks at the same frequency, and at this frequency, the coherence is higher than 0.7.

### 5. Pi2 PULSATIONS WHERE $L < 4$

In this section, we examined twenty two clear Pi2 pulsations, detected by the fluxgate magnetometer of the VAP-A and VAP-B near the perigee ( $L < 4$ ) for the same period (2012-2014). KAK is chosen as a reference station to determine the relative amplitude and phase of the Pi2 observed by VAP-A and VAP-B. Table 1 displays a list of twenty two Pi2: event number, date, start time, end time, VAP, L-value, and MLT of VAP. We have made four clear case studies of Pi2 where  $L < 4$  (at the onset time of Pi2). In each column, in Figs. 7(a)-7(d), top panel shows the time series plot of the  $\delta H$  component at KAK and the  $\delta Bz$  components of VAP, second panel shows the power spectra, the third panel shows the coherence, and the cross phase is plotted in the fourth panel. We removed a second-order polynomial of  $\delta Bz$  components fitted to the original time series using least-squares method. During 1815-1835 UT on 7 October 2012 the VAP-A was in north of the magnetic equator with a magnetic latitude 3.3, and it moved outward from  $L = 1.3$  to  $L = 2$  from premidnight to postmidnight (MLT = 2225-0125) while KAK was in postmidnight (MLT = 0315-0335). On 27 February 2013, during 2045-2100 UT, the VAP-A was in south of the magnetic equator with a magnetic latitude between -5.2 and -6.7, and it moved outward from  $L = 2.2$  to  $L = 2.4$  premidnight (MLT= 2005-2035) and KAK was in dawn (MLT= 0545-0600). During 1320-1340 UT on 1 January 2013 the VAP-A was in south of the magnetic equator with a magnetic latitude around -14, and it moved outward from  $L = 3.2$  to  $L = 3.6$  midnight (MLT~ 0000) and KAK was in premidnight (MLT= 2120-2140). On 19 April 2013, during 1540-1605 UT, the VAP-A was in north of the magnetic equator with a magnetic latitude around 2, and it moved inward from  $L = 3.9$  to  $L = 3.4$  postmidnight (MLT~ 0200) while KAK was in midnight (MLT= 0040-0105).

**Table 1.** List of twenty two Pi2 pulsations detected from fluxgate magnetometers of VAP near perigee: event number, date, start time, end time, VAP type, L-value, and MLT of VAP

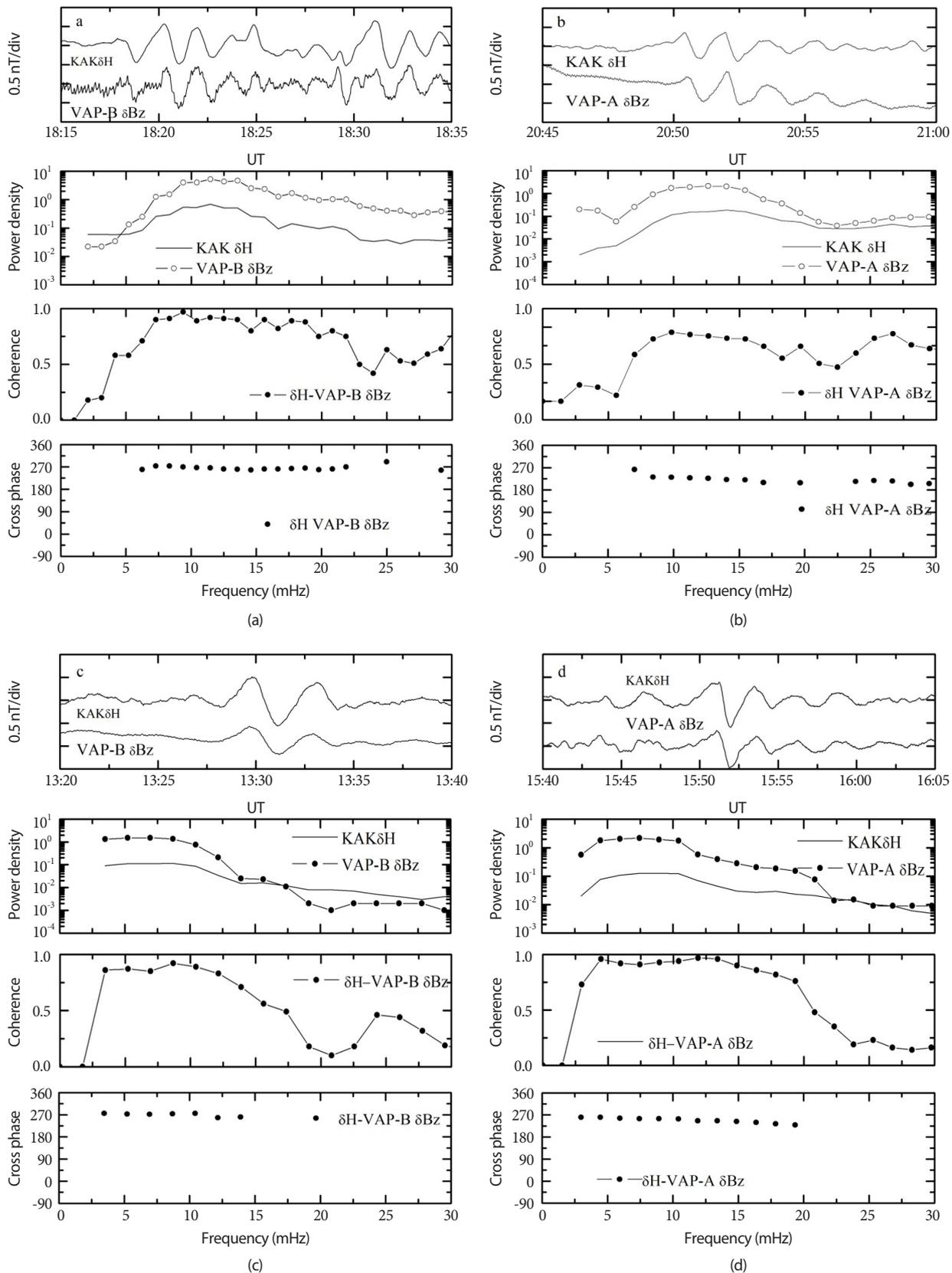
No.	Date yyyymmdd	Time (hh:mm UT) start - end	VAP type	L	MLT	No.	Date yyyymmdd	Time (hh:mm UT) start - end	VAP type	L	MLT
1	20121007	1815-1835	B	1.3	22:25	12	20130122	1410-1418	A	3	22:48
2	20121112	1210-1230	A	2.7	01:50	13	20130224	1458-1508	B	3.7	04:07
3	20121208	1625-1655	A	2.2	23:30	14	20130227	2045-2100	A	2.2	19:56
4	20121222	0945-0955	B	3.1	00:44	15	30130227	2110-2120	A	2.8	21:16
5	20121228	1225-1250	A	2.5	23:26	16	30130313	1712-1725	A	2.6	20:19
6	20121231	1210-1230	A	2.3	22:58	17	20130419	1548-1602	A	3.9	02:16
7	20121231	1900-1925	B	2.2	22:15	18	20130419	1030-1042	B	3.1	03:26
8	20130101	1325-1337	B	3.2	23:59	19	20130703	1520-1530	B	3.9	23:17
9	20130105	1815-1845	A	3.3	23:32	20	20131019	1455-1508	A	2.9	21:34
10	20130105	1630-1655	B	2.7	22:48	21	20131019	1455-1508	B	3.1	21:05
11	20130122	1420-1430	A	3.4	23:15	22	20140422	2035-2045	A	2.5	05:32

## 6. DISCUSSION

Satellite observation of magnetic pulsation, Pi2, at sub-storm onset at  $L > 6.6$  are well documented (Arthur & McPherron 1977). One of the objectives of the present study is to statistically examine Pi2 pulsations observed during the most quiet geomagnetic conditions ( $K_p = 0$ ) where  $L < 6$  at VAP-A and VAP-B satellites. While  $K_p = 0$ , we could consider the magnetosphere to be in a near ground state. Most of Pi2 pulsations were detected without sudden decreases in AL index. We found that seventy five events had high coherence between VAP-Bz and H components at KAK station. We also, found that 77 % of events were observed in the range between 5 and 12 mHz, which is smaller than the typical Pi2 power range of 6.7-25 mHz. It is known that the radially trapped fast mode waves in the plasmasphere are one of the source mechanism of low-latitude Pi2 pulsations. The evidence for the plasmaspheric resonance mode has been provided from satellite observations in the inner magnetosphere (e.g., Takahashi et al. 1995). The size of the plasmasphere is considered as one of the factors that controls the plasmaspheric resonance frequency. Takahashi et al. (2003) showed that Pi2 frequency decreases as the plasmopause distance determined using electron density data from a spacecraft, increases and that Pi2 frequencies are in the range of ~4-8 mHz (periods from 125 to 250 sec) when the plasmopause is above  $L = 6$ . Chappell et al. (1970) suggested a relationship between the  $K_p$  index and the plasmopause distance. From this relationship, it can be expected that the plasmopause is located somewhere above  $L = 6$  for  $K_p = 1$ . There is another feature of low-latitude Pi2 pulsations that it depends on the local time as shown in the Pi2 pulsation power distribution. As shown in Fig. 6, the Pi2 power data based on local time indicate that four Pi2 power has the maximum value at 20-23 MLT, and the asymmetry of Pi2 power occurs around the midnight. This result is similar to the result of Takahashi & Liou (2004). The Pi2 pulsation power depending on local time is higher in the pre-midnight portion

(Takahashi & Liou 2004). This is because the highest point of auroral power is around 21 LT and the source region of Pi2 pulsations is located near the eastern head of auroral surge. However, the exact cause is not yet identified. In this study, only four Pi2 pulsation powers were higher in the pre-midnight portion than in the post-midnight portion, six Pi2 pulsation power spectra showed the higher value in post-midnight portion, and the highest Pi2 pulsation power spectrum was observed between 20 and 23 MLT.

Another target of this study is to search the space magnetic data for clean Pi2 pulsations where  $L < 4$ . In space, the electric field data are sensitive to Pi2 pulsations down to  $L \sim 2$  but the magnetic field data are very noisy to investigate Pi2 pulsations at  $L < 4$  (Takahashi et al. 2003). That's why the Pi2 observation from magnetic data near satellite perigee did not attract any attention. In this study, fortunately, we could obtain twenty two clean Pi2 pulsation by the fluxgate magnetometer of the VAP-A and VAP-B near perigee ( $L < 4$ ). The compressional components showed Pi2 oscillations on L shells as low as ~1. This enabled us to see the relationship among the compressional components at VAP and H component at KAK for events observed at various L distances. We found that the compressional components at VAP of all events have high coherence with H component at KAK with nearly identical waveforms. We presented four example of Pi2 oscillations on different L shells ( $L < 4$ ). The four examples show similar spectral characteristics (Figs. 7(a)-7(d)). All the  $\delta B_z$  data give a power spectrum nearly identical to the  $\delta H$  spectrum in the frequency band range from 5 to 20 mHz. The cross phase between KAK  $\delta H$  and VAP- $\delta B_z$  is about  $270^\circ$  in all cases. It should be noted that this study, related to Pi2 near perigee, is to show the possibility to detect Pi2 events from space magnetometer where  $L < 4$  with high coherence of compressional components with ground H component. However, twenty two events are not enough to find out the mode structure of these events. We need to extend our study to cover more data sets focusing on events near perigee.



**Fig. 7.** Four case studies of Pi2 pulsations near perigee (a) L = 1.3 on 7 October 2012, (b) L = 2.2 on 27 February 2013, (c) L = 3.2 on 1 January 2013, and (d) L = 3.9 on 19 April 2013.

Integrated interpretation of magnetic field data from the magnetosphere, ionosphere and ground can lead to better understanding of Pi2 wave occurrence and propagation. Thus, other studies of Pi2 events recorded simultaneously in several locations of the geospace are necessary and a mission like Swarm in the topside ionosphere, is expected to help with resolving a lot of Pi2 issues. Presently, a study is under progress on the relationship between Pi2 occurrence in the low-latitude and the magnetic field measured by VAP and Swarm satellites.

## 7. CONCLUSION

A statistical analysis of the Pi2 pulsations has been made using the VAP-A and VAP-B satellites when  $K_p = 0$  from October 2012 to December 2014. During this period, ninety six events were detected. In this study, seventy five events had high coherence between VAP-Bz and H components at the KAK station. We found that 77 % of the events had a power spectrum between 5 and 12 mHz, which differs from the regular Pi2 band range from 6.7 to 25 mHz. In addition, this study demonstrates that it is possible to observe Pi2 pulsations from space fluxgate magnetometers near perigee. Twenty two clean Pi2 pulsations were detected and listed using the Van Allen probe fluxgate magnetometer where  $L < 4$ . Four examples of Pi2 oscillations on different L shells near perigee were presented. The four examples show similar spectral characteristics.

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## REFERENCES

- Allan W, White SP, Poulter EM, Impulse-excited hydromagnetic cavity and field-line resonances in the magnetosphere, *Planet. Space Sci.* 34, 371-385 (1986). [https://doi.org/10.1016/0032-0633\(86\)90144-3](https://doi.org/10.1016/0032-0633(86)90144-3)
- Arthur CW, McPherron RL, Micropulsations in the morning sector, 3. Simultaneous ground-satellite observations of 10- to 45-s period waves near  $L = 6.6$ , *J. Geophys. Res.* 82, 2859-2866 (1977). <https://doi.org/10.1029/JA082i019p02859>
- Chappell CR, Harris KK, Sharp GW, A study of the influence of magnetic activity on the location of the plasmapause as measured by OGO 5, *J. Geophys. Res.* 75, 50-56 (1970). <https://doi.org/10.1029/JA075i001p00050>
- Clauer CR, McPherron RL, Mapping the local time-universal time development of magnetospheric substorms using mid-latitude magnetic observations, *J. Geophys. Res.* 79, 2811-2820 (1974). <https://doi.org/10.1029/JA079i019p02811>
- Fujita S, Glassmeier KH, Magnetospheric cavity resonance oscillations with energy flow across the magnetopause, *J. Geomagn. Geoelectr.* 47, 1277-1292 (1995). <https://doi.org/10.5636/jgg.47.1277>
- Ghamry E, Morningside Pi2 pulsation observed in space and on the ground, *J. Astron. Space Sci.* 32, 305-310 (2015). <https://doi.org/10.5140/JASS.2015.32.4.305>
- Ghamry E, Fathy A, A new method to calculate the time delay of the Pi2 pulsations, *Adv. Space Res.* 57, 701-709 (2016). <https://doi.org/10.1016/j.asr.2015.10.045>
- Ghamry E, Mahrous A, Yasin N, Fathy A, Yumoto K, First investigation of geomagnetic micropulsation, Pi2, in Egypt, *Sun Geosph.* 6, 84-87 (2011).
- Ghamry E, Mahrous A, Fathy A, Salama N, Yumoto K, Signatures of the low-latitude Pi2 pulsations in Egypt, *NRIAG J. Astron. Geophys.* 1, 45-50 (2012). <https://doi.org/10.1016/j.nrjag.2012.11.005>
- Ghamry E, Kim KH, Kwon HJ, Lee DH, Park JS, et al., Simultaneous Pi2 observations by the Van Allen Probes inside and outside the plasmasphere, *J. Geophys. Res.* 120, 4567-4575 (2015). <https://doi.org/10.1002/2015JA021095>
- Kepko L, Kivelson M, Generation of Pi2 pulsations by bursty bulk flows, *J. Geophys. Res.* 104, 25021-25034 (1999). <https://doi.org/10.1029/1999JA900361>
- Kletzing CA, Kurth WS, Acuna M, MacDowall RJ, Torbert RB, et al., The electric and magnetic field instrument suite and integrated science (EMFISIS) on RBSP, *Space Sci. Rev.* 179, 127-181 (2013). <https://doi.org/10.1007/s11214-013-9993-6>
- Kwon HJ, Kim KH, Jun CW, Takahashi K, Lee DH, et al., Low-latitude Pi2 pulsations during intervals of quiet geomagnetic conditions ( $K_p \leq 1$ ), *J. Geophys. Res.* 118, 6145-6153 (2013). <https://doi.org/10.1002/jgra.50582>
- Kwon HJ, Kim KH, Jee G, Park JS, Jin H, et al., Plasmapause location under quiet geomagnetic conditions ( $K_p \leq 1$ ): THEMIS observations, *Geophys. Res. Lett.* 42, 7303-7310 (2015). <https://doi.org/10.1002/2015GL066090>
- Lee DH, Dynamics of MHD wave propagation in the low-latitude magnetosphere, *J. Geophys. Res.* 101, 15371-15386 (1996). <https://doi.org/10.1029/96JA00608>
- Lee DH, On the generation mechanism of Pi2 pulsations in the magnetosphere, *Geophys. Res. Lett.* 25, 583-586 (1998). <https://doi.org/10.1029/98GL50239>
- Lyons LR, Nagai T, Blanchard GT, Samson JC, Yamamoto T,

- et al., Association between Geotail plasma flows and auroral poleward boundary intensifications observed by CANOPUS photometers, *J. Geophys. Res.* 104, 4485-4500 (1999). <https://doi.org/10.1029/1998JA900140>
- Mauk BH, Fox NJ, Kanekal SG, Kessel RL, Sibeck DG, et al., Science objectives and rationale for the radiation belt storm probes mission, *Space Sci. Rev.* 179, 3-27 (2013). <https://doi.org/10.1007/s11214-012-9908-y>
- Sutcliffe PR, The association of harmonics in Pi2 power spectra with the plasmopause, *Planet Space Sci.* 23, 1581-1587 (1975). [https://doi.org/10.1016/0032-0633\(75\)90085-9](https://doi.org/10.1016/0032-0633(75)90085-9)
- Sutcliffe PR, Yumoto K, Dayside Pi2 pulsations at low latitudes, *Geophys. Res. Lett.* 16, 887-890 (1989). <https://doi.org/10.1029/GL016i008p00887>
- Sutcliffe PR, Yumoto K, On the cavity mode nature of low-latitude Pi2 pulsations, *J. Geophys. Res.* 96, 1543-1551 (1991). <https://doi.org/10.1029/90JA02007>
- Takahashi K, Liou K, Longitudinal structure of low-latitude Pi2 pulsations and its dependence on aurora, *J. Geophys. Res.* 109, A12206 (2004). <https://doi.org/10.1029/2004JA010580>
- Takahashi K, Ohtani S, Anderson BJ, Statistical analysis of Pi2 pulsations observed by the AMPTE CCE spacecraft in the inner magnetosphere, *J. Geophys. Res.* 100, 21929-21942 (1995). <https://doi.org/10.1029/95JA01849>
- Takahashi K, Ohtani S, Hughes WJ, Anderson RR, CRRES observation of Pi2 pulsations: wave mode inside and outside the plasmasphere, *J. Geophys. Res.* 106, 15567-15581 (2001). <https://doi.org/10.1029/2001JA000017>
- Takahashi K, Lee DH, Nosé M, Anderson RR, Hughes WJ, CRRES electric field study of the radial mode structure of Pi2 pulsations, *J. Geophys. Res.* 108, 1210 (2003). <https://doi.org/10.1029/2002JA009761>
- Teramoto M, Takahashi K, Nosé M, Lee DH, Sutcliffe PR, Pi2 pulsations in the inner magnetosphere simultaneously observed by the active magnetospheric particle tracer explorers/charge composition explorer and dynamics explorer 1 satellites, *J. Geophys. Res.* 116, A07225 (2011). <https://doi.org/10.1029/2010JA016199>
- Wygant JR, Bonnell JW, Goetz K, Ergun RE, Mozer FS, et al., The electric field and waves instruments on the radiation belt storm probes mission, *Space Sci. Rev.* 179, 183-220 (2013). <https://doi.org/10.1007/s11214-013-0013-7>
- Yeoman TK, Orr D, Phase and spectral power of mid-latitude Pi2 pulsations: evidence for a plasmaspheric cavity resonance, *Planet. Space Sci.* 37, 1367-1383 (1989). [https://doi.org/10.1016/0032-0633\(89\)90107-4](https://doi.org/10.1016/0032-0633(89)90107-4)
- Zhu X, Kivelson MG, Global mode ULF pulsations in a magnetosphere with a nonmonotonic Alfvén velocity profile, *J. Geophys. Res.* 94, 1479-1485 (1989). <https://doi.org/10.1029/JA094iA02p01479>